



**BME**

Budapesti Műszaki és Gazdaságtudományi Egyetem



**KJKIT**

Közlekedésmérnöki és Járműmérnöki Kar

Közlekedés- és Járműirányítási Tanszék

# Environment Sensing

## Lecture 6

### Environment Representation and Static Occupancy Grid Maps

Dr. Tamás Bécsi

# Introduction

- One of the key challenges of any (AD) system lies in the perception and **representation** of the driving environment
- Semantical/Cognitive representation of the world is hard
- Environment representation is the buzzword version of mapping (in our scope). Since mapping can be either spatial or temporal, dynamic or static.

# The „ideal” environment representation

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- **Provides all information** necessary for implementing any ADAS or AD function
- **Compact enough** for transmission between electronic control units or V2V/V2I communication interfaces
- Is **generable real-time** in a computationally inexpensive, robust way with respect to sensor errors/malfunctions
- **Suppress irrelevant** environment **details** to facilitate situation interpretation and planning approaches
- **Represent free space** explicitly to permit safety-related trajectory planning
- Is able to handle **static and dynamic** objects
- Allow to incorporate **uncertainties**

# Mapping is pre-computation

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Közlekedés- és Járműirányítási Tanszék

- From the point of view of self-driving technology, the mapping operation includes everything we can do to pre-compute things before the AV starts driving.
- Perception and localization of static objects in the world such as roads, intersections, street signs, etc. can be solved offline and in a highly accurate manner.
- **Without it, the AD/ADAS function has to figure out the whole background at the instant**

# Mapping improves safety

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Közlekedés- és Járműirányítási Tanszék

- The use of maps for navigation is OK
- Though maps could adopt pragmatic best practices that reduce risk during driving
  - E.g. providing not only speed limits, but speed profiles
  - The vehicle can precondition itself for situations



# Map is a unique sensor

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Közlekedés- és Járműirányítási Tanszék

- Has no range limitations
- It is immune to runtime occlusion from dynamic objects
- Can also be used for sensor fusion





# Map can be a global shared state

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Közlekedés- és Járműirányítási Tanszék

- Just as any other Cloud service.
- Like a large full-information MMO game



# Hierarchical approach



## Dynamic

- Updated Real-time
- Nearby vehicles, pedestrians, traffic signs

## Semi-dynamic

- Minute based
- Accidents, congestions, road works, weather

## Semi-static

- Hourly
- planned traffic/regulation changes, weather forecast

## Static

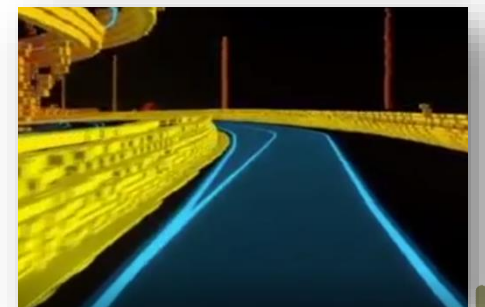
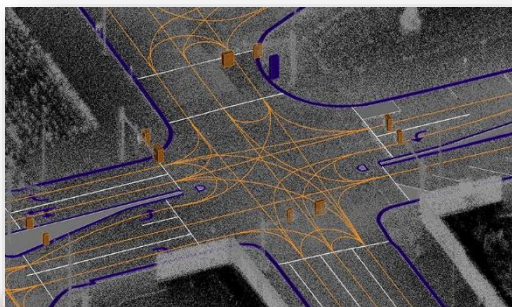
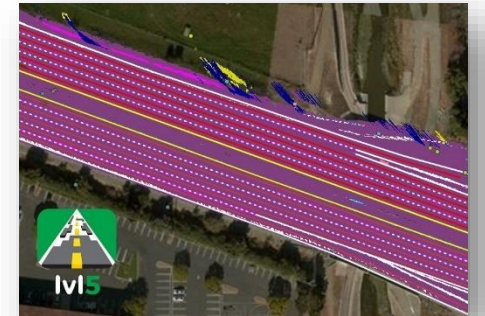
- Monthly
- Roads/lanes/3D structure (Basically the SD map)



# HD maps

- Many participants,
- Not this course...
  - Localization and mapping
  - ADAS
  - etc...

- HERE
- DeepMap
- Civil Maps
- Carmera
- TomTom
- Ivl5
- Baidu

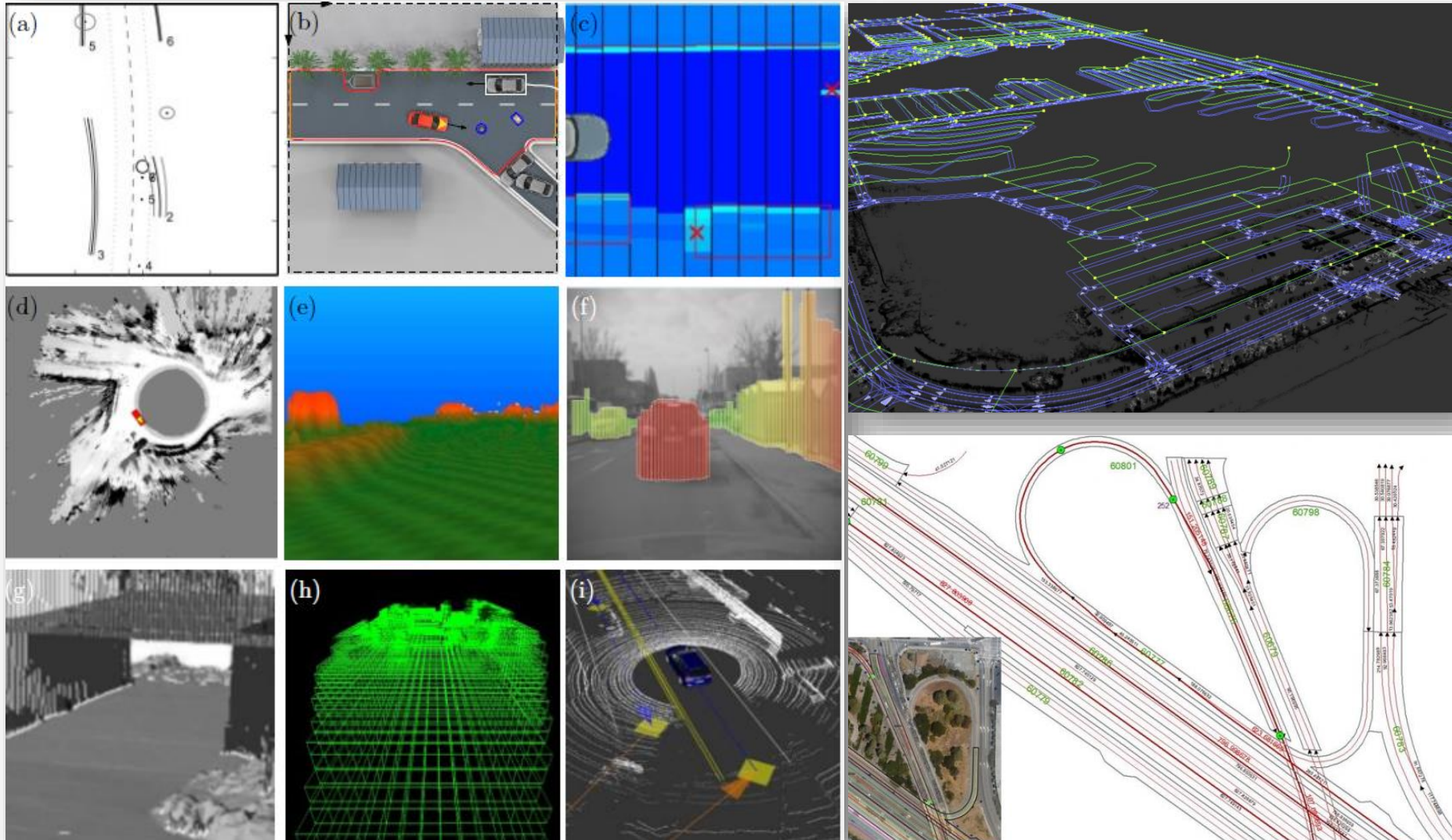


# Feature, Volumetric, Semantic

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Közlekedés- és Járműirányítási Tanszék



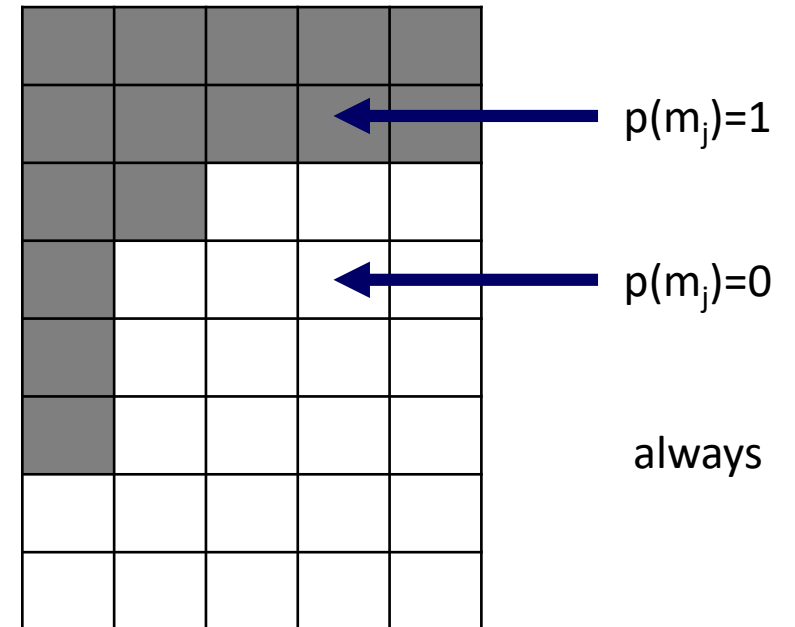
# Feature Maps vs Grid Maps

- Natural choice for Kalman filter-based SLAM systems
- Compact representation
- Multiple feature observations improve the position estimate (EKF)
- Discretize the world into cells
- Grid structure is rigid
- Each cell is assumed to be occupied or free space
- Non-parametric model
- Require substantial memory resources
- Does not rely on a feature detector



# Grid maps basics

- The area is simplified to 2D space,
- With equidistant grid,
- And each grid cell is a binary random variable, that models occupancy
  - Occupied:  $p(m_j)=1$
  - Unoccupied:  $p(m_j)=0$
  - Unknown:  $p(m_j)=0.5$
- The grid is assumed to be static
- All cells have independent probability





# Basics recap

- $m$  – the map,  $p(m)$  assumption
- $m_i$  – one cell in the map,  $p(m_i)$  assumption
  - $p(m) = \prod p(m_i)$
- $z_t$  - measurement in step  $t$
- $z_{1:t} = \{z_1, z_2 \dots z_t\}$  set of measurements from step 1 to  $t$
- All measurement are independent!
  - $p(z_2) = p(z_2|z_1)$  the current measurement is independent for all previous:  $p(z_t) = p(z_t|z_{1:t-1})$
- $x_t$  - the state of the sensor in step  $t$

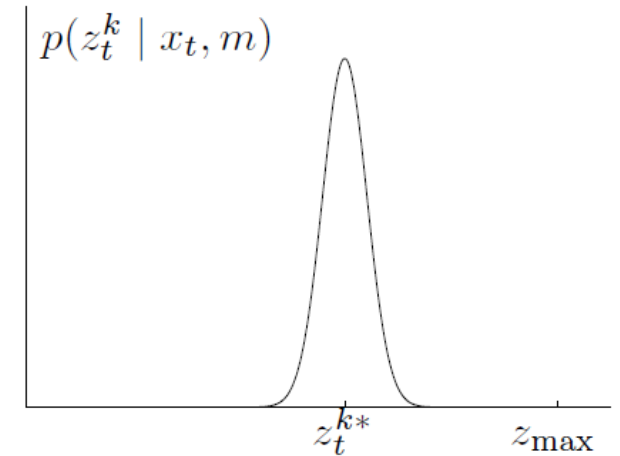
# The sensor model of a proximity sensor

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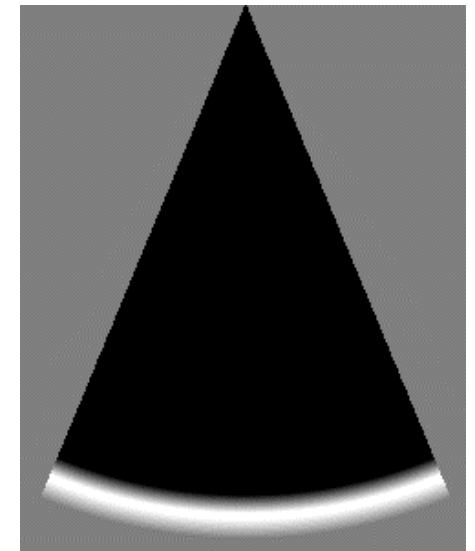
Közlekedés- és Járműirányítási Tanszék

- The Sensor model states that
  - given a map  $m$  (actually the reality)
  - and a sensor state  $x_t$
  - what is the probability function of the measurement?



$$p(z_t | x_t, m)$$

- Simply: What is the sensor output in a given scenario?



# The inverse sensor model of a proximity sensor

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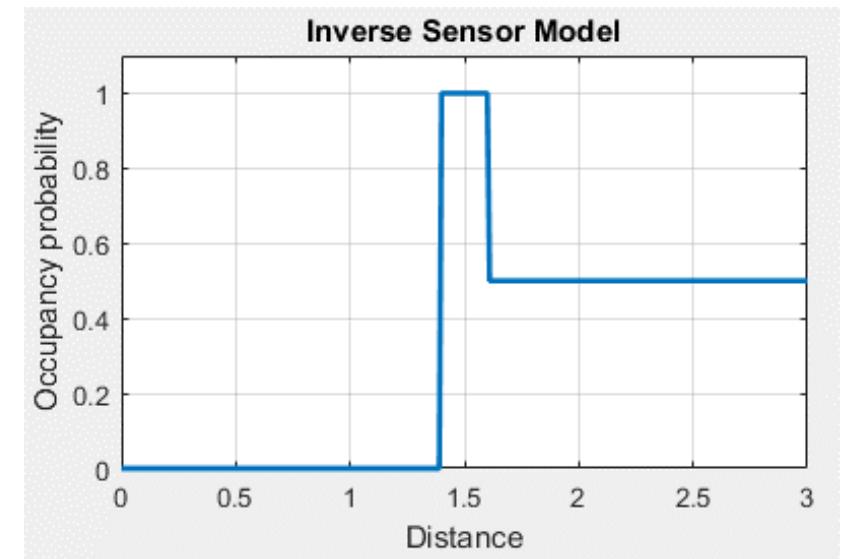
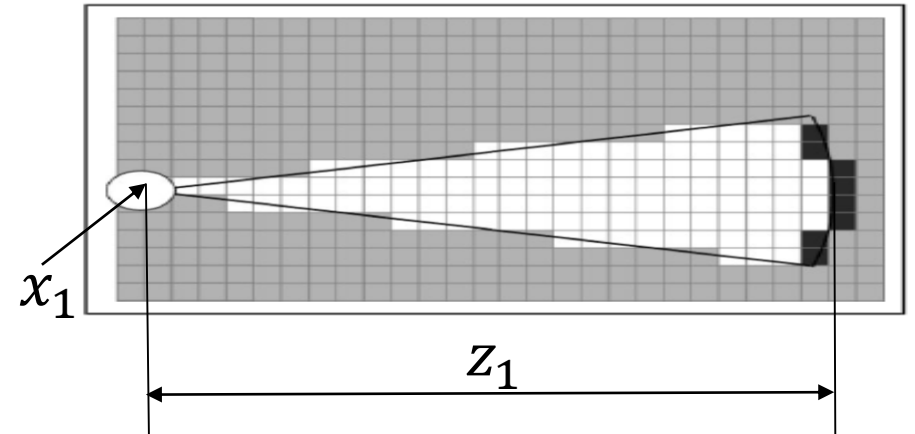
Közlekedésmérnöki és Járműmérnöki Kar

Közlekedés- és Járműirányítási Tanszék

- The Inverse Sensor model states that
  - given a measurement  $z_t$
  - and a sensor state  $x_t$
  - what is the probability function for the map cell  $m_i$ ?

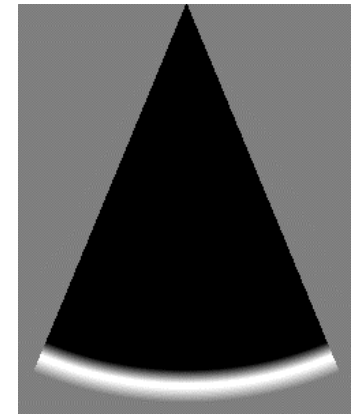
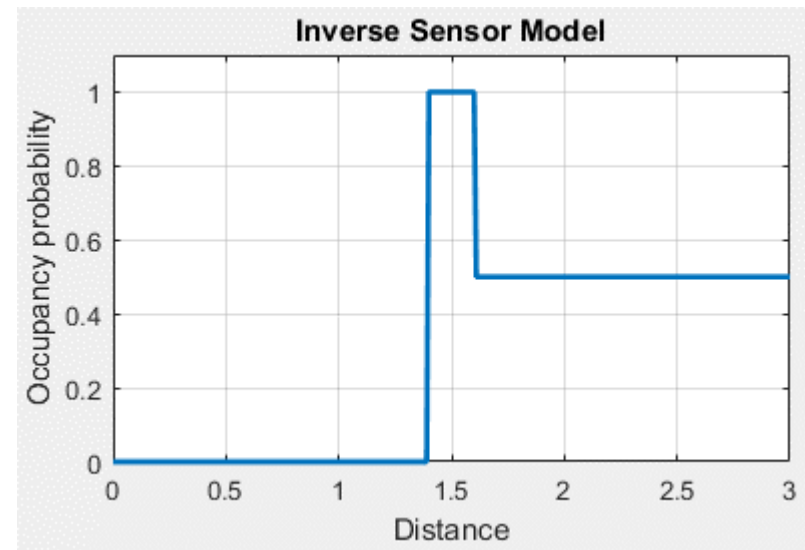
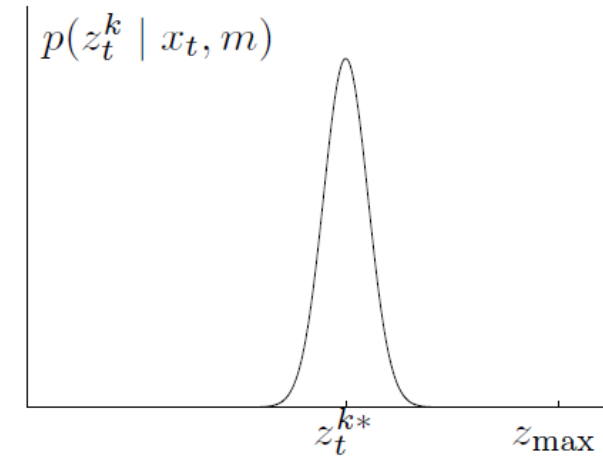
$$p(m_i | z_t, x_t)$$

- Simply: What is the sensor output in a given scenario?



# Mapping, „Naive” Approach 1.

- The sensor model for mapping is considered deterministic, with minimal noise on measurement
- The inverse sensor model states, that the sensor output has small deviation from the actual distance of the closest object.





# Mapping, Naive Approach 2.

- Without any probabilistic approach,
  1. Initialize Map with unknown state for each cell (0.5)
  2. Update each map cell  $m_j$  with its corresponding measurement  $z_j$  by following the rule:

$m_j \backslash z_j$	0	0.5	1
0	0	0	0
0.5	0	0.5	1
1	0	1	1

# Demo

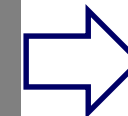
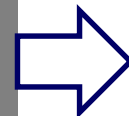
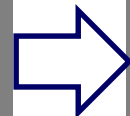
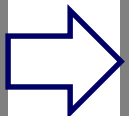
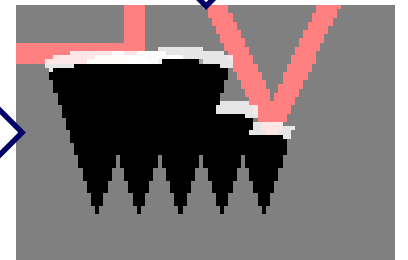
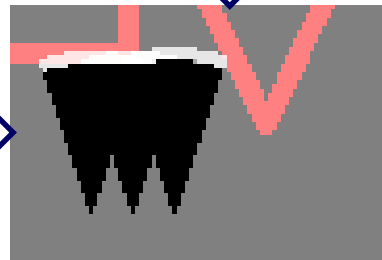
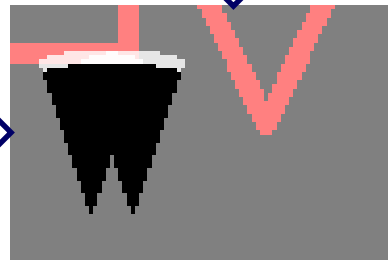
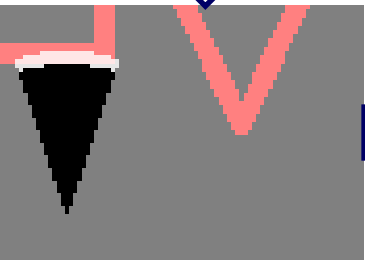
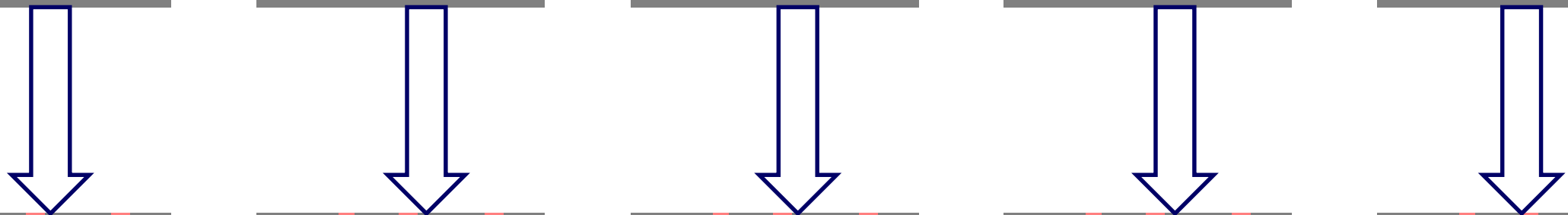
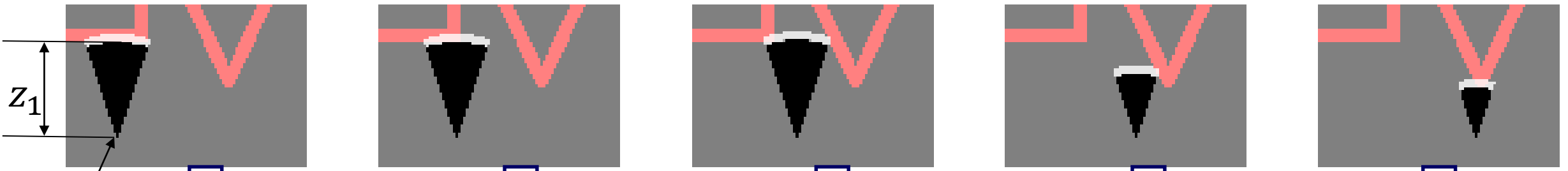
*inverse sensor model*

$$p(m|z_1, x_1)$$

$$p(m|z_2, x_2)$$

...

$$p(m|z_t, x_t)$$



$$p(m|z_1, x_1)$$

$$p(m|z_{1:2}, x_{1:2})$$

...

$$p(m|z_{1:t}, x_{1:t})$$

# Demonstration Videos

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Közlekedés- és Járműirányítási Tanszék

1. Ideal Sensor

...

2. What if, we have Gaussian noise on the sensor?

...

And more...

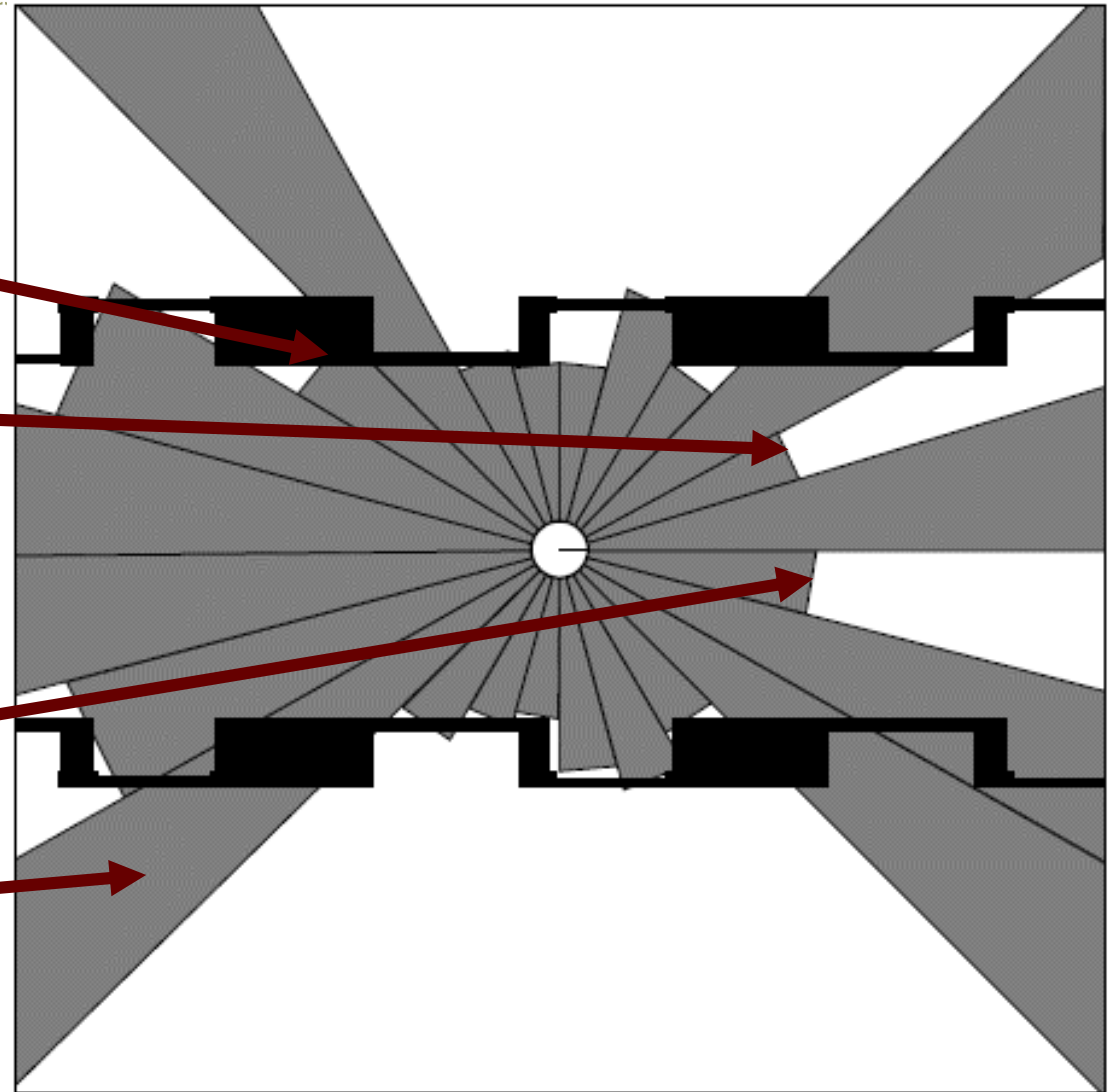
# The Problem with the Naive approach

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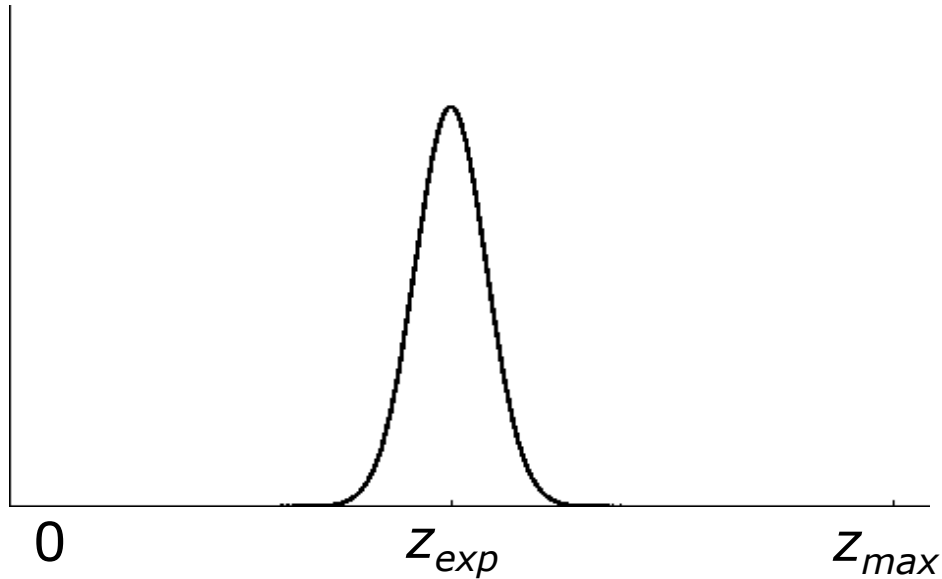
- Beams reflected by obstacles
- Beams reflected by persons / caused by crosstalk
- Random measurements
- Maximum range measurements





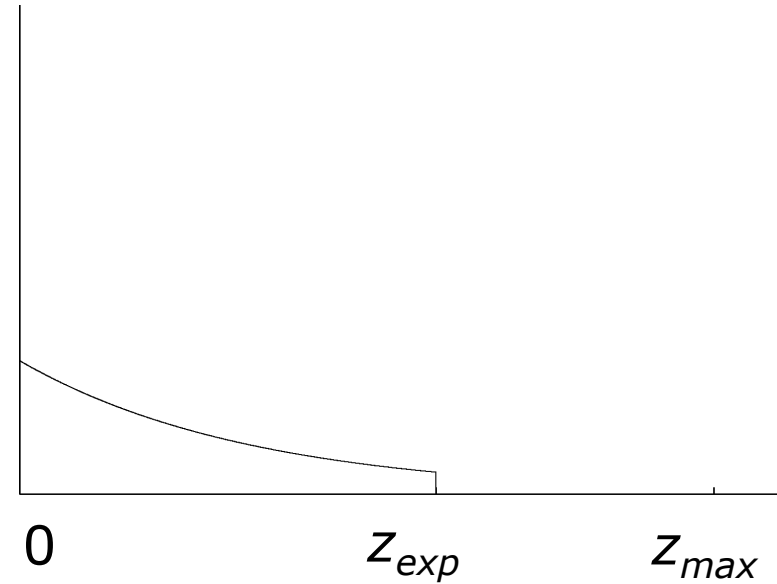
# Sensor errors

## Measurement noise



$$P_{hit}(z | x, m) = \eta \frac{1}{\sqrt{2\pi b}} e^{-\frac{1}{2} \frac{(z - z_{exp})^2}{b}}$$

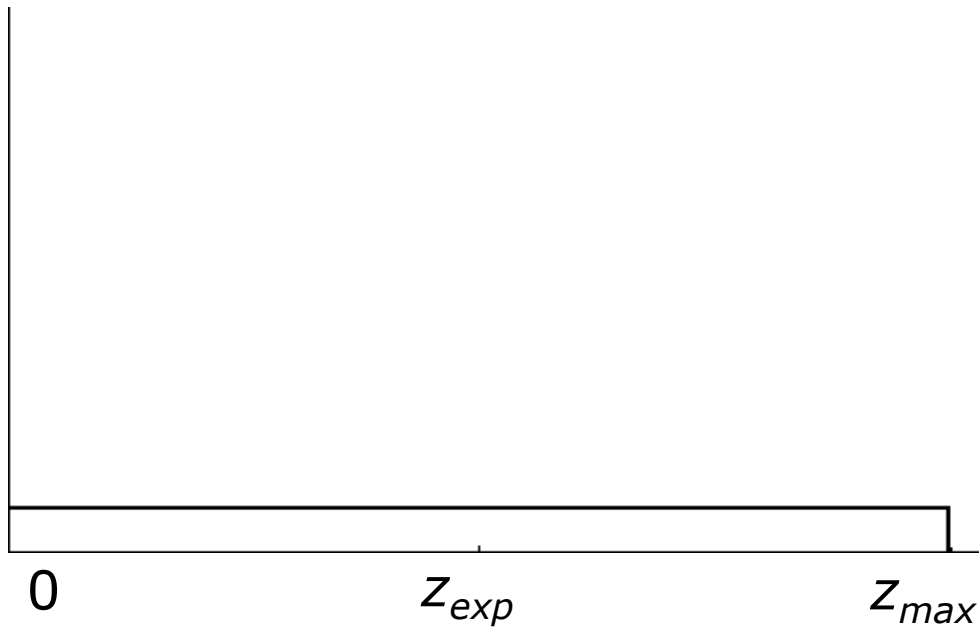
## Unexpected obstacles



$$P_{unexp}(z | x, m) = \begin{cases} \eta \lambda e^{-\lambda z} & z < z_{exp} \\ 0 & otherwise \end{cases}$$

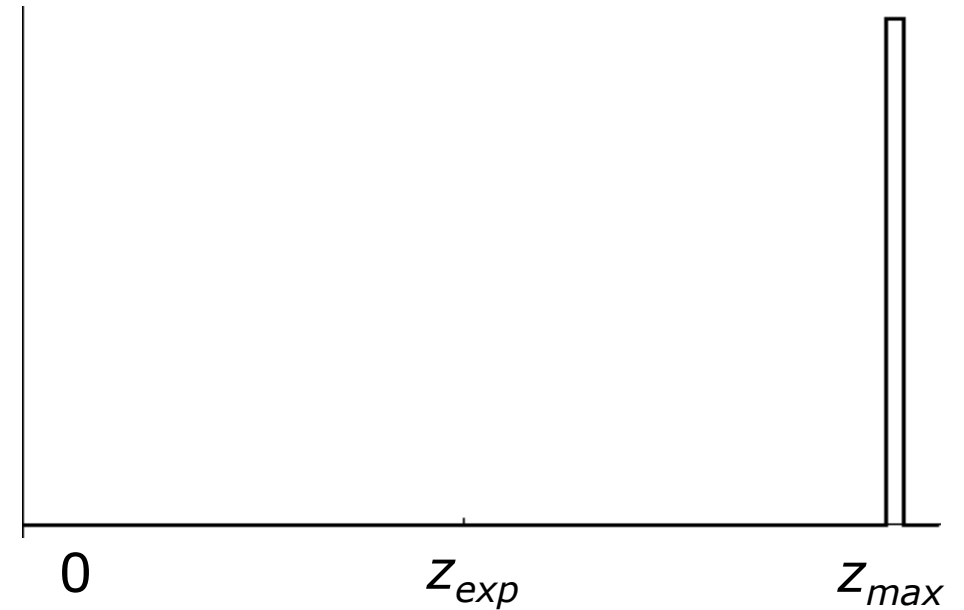
# Sensor Errors

Random measurement



$$P_{rand}(z | x, m) = \eta \frac{1}{z_{max}}$$

Max range



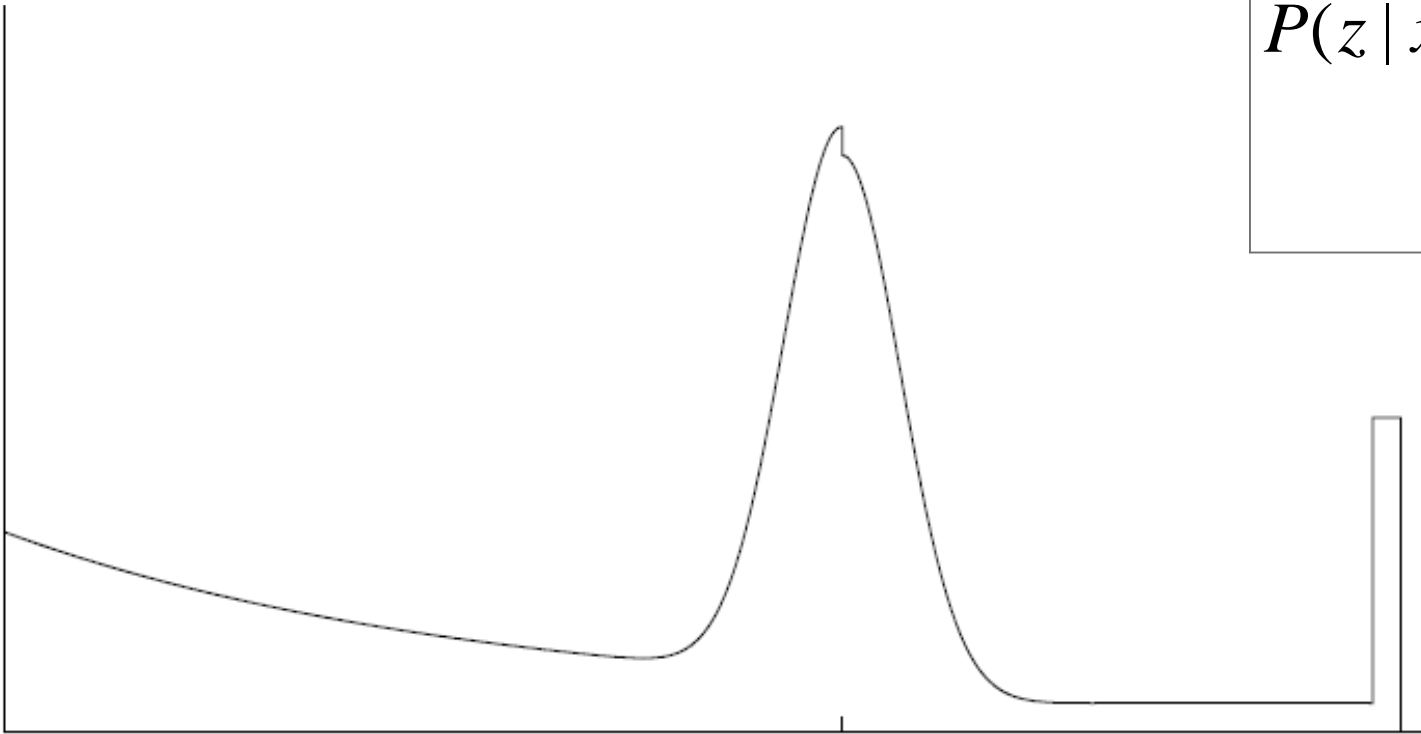
$$P_{max}(z | x, m) = \eta \frac{1}{z_{small}}$$

# Resulting Mixture Density/Sensor modell

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$$P(z | x, m) = \begin{pmatrix} \alpha_{\text{hit}} \\ \alpha_{\text{unexp}} \\ \alpha_{\text{max}} \\ \alpha_{\text{rand}} \end{pmatrix}^T \cdot \begin{pmatrix} P_{\text{hit}}(z | x, m) \\ P_{\text{unexp}}(z | x, m) \\ P_{\text{max}}(z | x, m) \\ P_{\text{rand}}(z | x, m) \end{pmatrix}$$

# Demonstration Video

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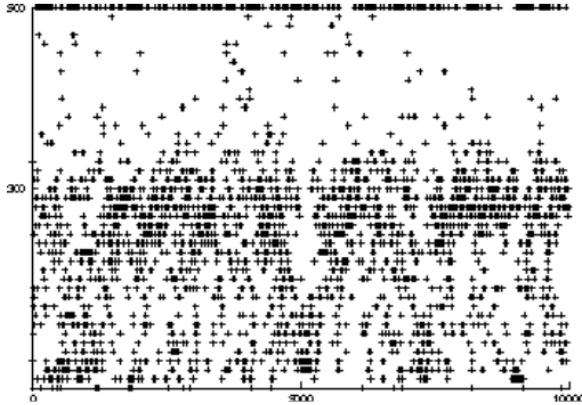
Közlekedésmérnöki és Járműmérnöki Kar

Közlekedés- és Járműirányítási Tanszék

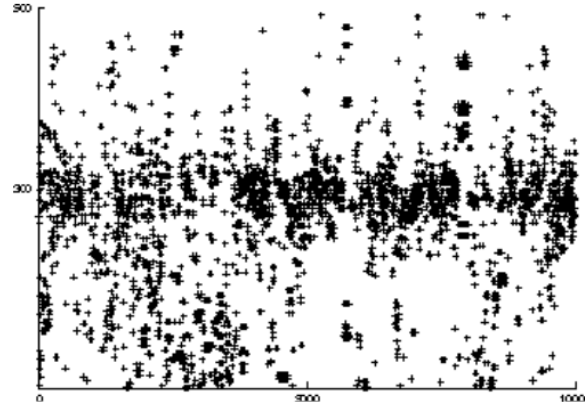
- With complex sensor error scheme



# Determine model



Sonar

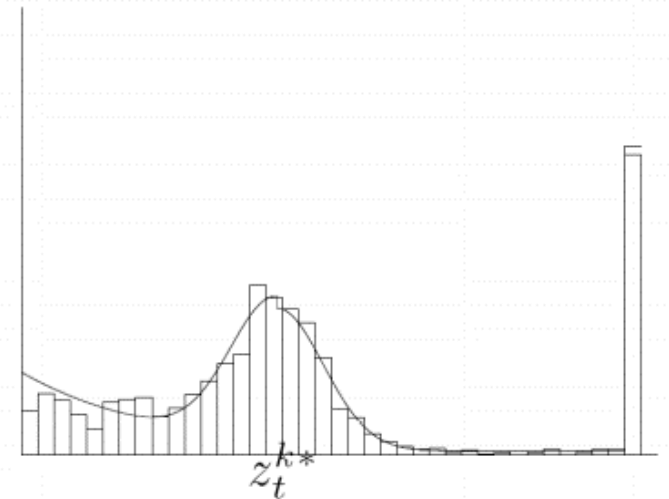
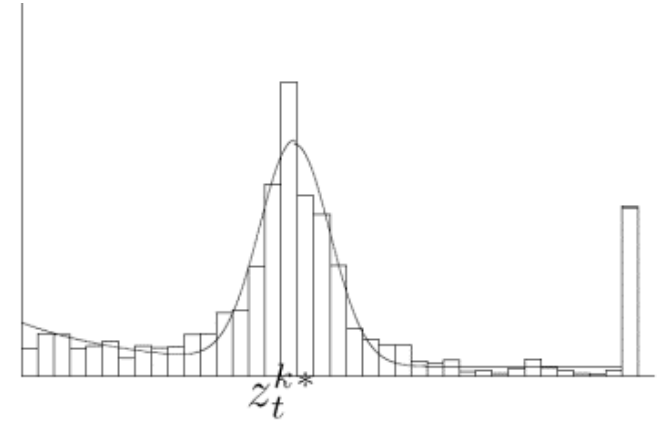


Laser

## Mixture of

- a Gaussian distribution with mean at distance to closest obstacle
- a uniform distribution for random measurements
- a small uniform distribution for max range measurements

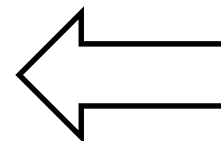
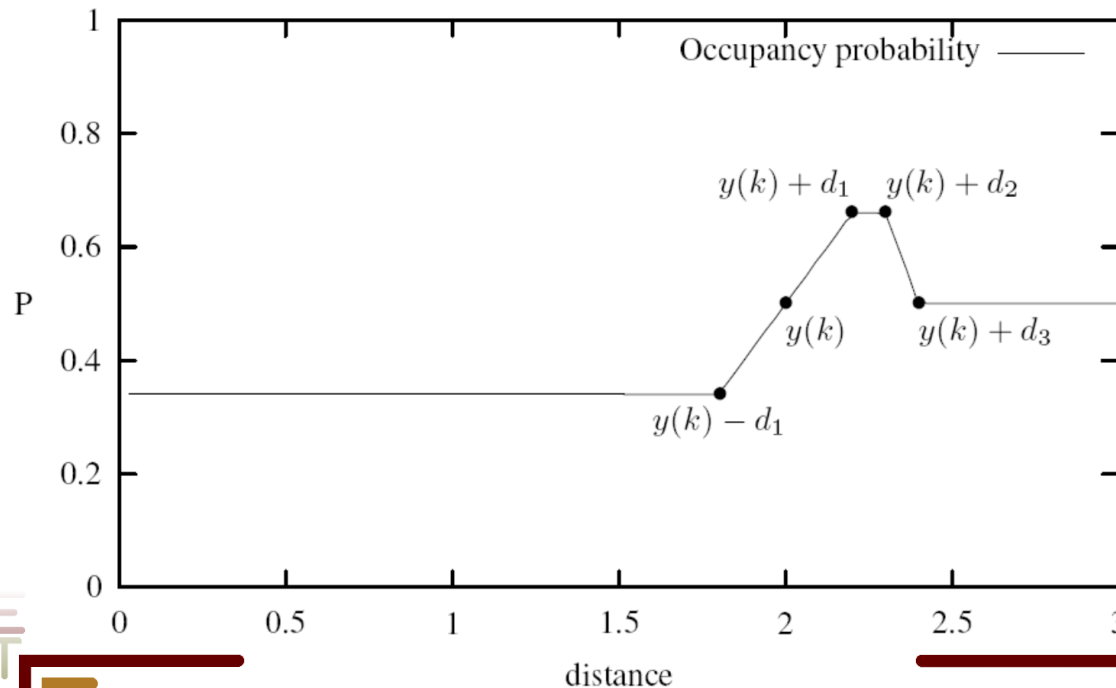
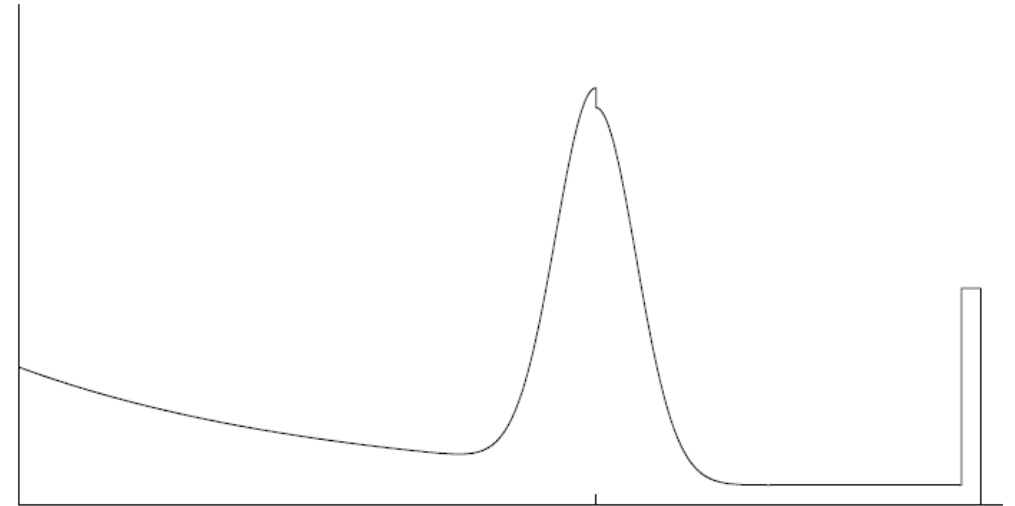
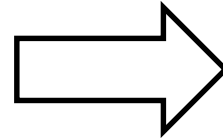
FIT





# Probabilistic grid mapping

The sensor model for mapping is as described previously



The inverse sensor model should also consider this

# Probabilistic grid mapping 1.

We want to determine the map  $m$ , based on all previous sensor states and measurements. Actually(1), since all cells are independent, we write the term for one cell:

$$p(m_i | z_{1:t}, x_{1:t}) = \frac{p(z_t | m_i, z_{1:t-1}, x_{1:t}) p(m_i | z_{1:t-1}, x_{1:t})}{p(z_t | z_{1:t-1}, x_{1:t})}, \text{ by applying the Bayes Rule}$$

Actually(2), since we won't do anything with the sensor position mathematically, we omit it to make things clearer:

$$p(m_i | z_{1:t}) = \frac{p(z_t | m_i, z_{1:t-1}) p(m_i | z_{1:t-1})}{p(z_t | z_{1:t-1})}$$

# Estimating a Map From Data

$$p(m_i | z_{1:t}) = \frac{p(z_t | m_i, z_{1:t-1}) p(m_i | z_{1:t-1})}{p(z_t | z_{1:t-1})}$$

the measurements are independent  
 $p(z_t | z_{1:t-1}) = p(z_t)$

$$p(m_i | z_{1:t}) = \frac{p(z_t | m_i) p(m_i | z_{1:t-1})}{p(z_t)}$$

another Bayes on  $p(z_t | m_i)$

$$p(m_i | z_{1:t}) = \frac{p(m_i | z_t) p(z_t) p(m_i | z_{1:t-1})}{p(m_i) p(z_t)}$$

simplify by  $p(z_t)$

$$p(m_i | z_{1:t}) = \frac{p(m_i | z_t) p(m_i | z_{1:t-1})}{p(m_i)}$$

# Estimating a Map From Data

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Current Measurement  
(From inverse sensor model)

Map Based on all previous  
measurements  
(Making the algorithm sequential)

$$p(m_i | z_{1:t}) = \frac{p(m_i | z_t) p(m_i | z_{1:t-1})}{p(m_i)}$$

Prior assumption on the map (generally 0.5)

Static State Binary Bayes Filter – Though multiplication causes some problems

# Further improvement

$$p(\neg m|z_{1:t}) = \frac{p(\neg m|z_t)p(\neg m|z_{1:t-1})}{p(\neg m)}$$

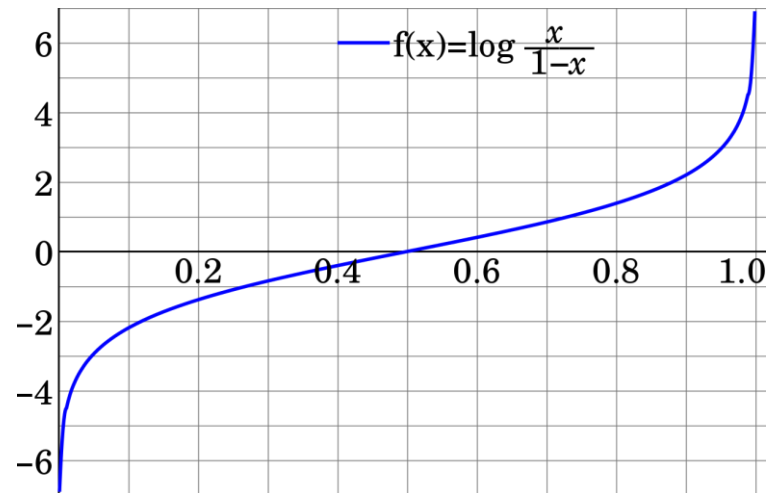
- Ratio of probabilities:

$$\frac{p(m|z_{1:t})}{p(\neg m|z_{1:t})} = \frac{p(m|z_{1:t})}{1 - p(m|z_{1:t})} = \frac{p(m|z_t)}{1 - p(m|z_t)} \frac{p(m|z_{1:t-1})}{1 - p(m|z_{1:t-1})} \frac{1 - p(m)}{p(m)}$$

Measurement                      Recursion                      Prior



# Using log odds notation



$$l(x) = \log \frac{p(x)}{1 - p(x)};$$

$$p(x) = \frac{1}{1 + \exp(l(x))}$$

$$l(m|z_{1:t}) = l(m|z_t) + l(m|z_{1:t-1}) - l(m)$$

$$l_t = \text{inverse.sensor.model} + l_{t-1} - l_0$$

- Demonstration video

# Summary

- Occupancy grid maps discretize the space into Independent cells
- Each cell is a binary random variable estimating if the cell is occupied
- Static state binary Bayes filter per cell
- Mapping with known poses is easy
- Log odds model is fast to compute
- No need for predefined features

# Summary II.

- „Known” poses is questionable
- Short term quasi-known poses are OK
- wide-angle sensors are still a problem, with biased measurements
- „independent cell”  $\leftrightarrow$  „independent measurement” assumption makes it weaker

# References

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